

PUMP SELECTION FOR A RESERVOIR SYSTEM

Hameed S. Salih

Civil Engineer

September 2015

Table of Contents

Introduction	Page 3
Design Procedure.....	Page 4
Theory	Page 6
Problem Statement	Page 7
Constants	Page 10
Conversions	Page 11
Calculations	Page 12
Conclusion	Page 18
Bibliography	Page 19
Table and Charts	Page 20

Introduction:

This project deals with a typical system in the area of hydraulic engineering. Delivering water between two points of an existed hydraulic reservoir system requires attention and careful consideration. First of all, it is necessary to know whether the system selected for the project is in compliance with engineering standards. Second, considering all the potential cases concerning safety, it is important also to determine how much the planned project or system is functional. Moreover, regardless of what is being dealt with the current plan under question, it is also essential to account for any other possible alternatives that may replace the current option on hand.

Design Procedure:

This project comprises of two reservoirs which are apart from each other by a certain distance and elevation. One reservoir supplies water to the second one through a line of pipe system and fittings. Two pumps are available from a manufacture company that is supposed to be the provider of the pumps for the project. Only one pump is needed to be fixed on the delivery system. It is required to choose between the two pumps. In addition, the manufacture company supplied the project superintendent with the characteristic data belonging to the pumps.

In this case, the design procedure for the selection process would be the following;

1. Taking advantage of discharge, head, and efficiency that are provided for both pumps, the characteristic curves for the two pumps can be drawn.
2. Considering the static head between the two reservoirs as well as the head loss through the delivery pipe, the system head can be determined and its curve can be drawn along with the characteristic curves for both the pumps.

3. The point where the system head crosses the pump head is operating point (OP). The extension of OP up to the point where intersects with the efficiency curve determines the OP efficiency.
4. The same procedure is followed for both the pumps.
5. The pump that gives the lease (BEP-OP) is considered to be the right pump for the project; as this indicates that the pump will operate with least power consumption while providing the required head that is needed for delivering water from one reservoir into the other.

Theory:

A. Pump System:

$$1. P = \frac{\gamma Q h_p}{\eta}$$

2. Develop characteristic curves

$$3. Z = \frac{P_{atm}}{\gamma} - h_{L_s} - \frac{P_v}{\gamma} - \sigma h_p$$

$$4. h_{p2} = h_{p1} \frac{N_2^2 d_2^2}{N_1^2 d_1^2} = h_{p1} \frac{N_2^2}{N_1^2}$$

$$P_2 = P_1 \frac{N_2^3 d_2^5}{N_1^3 d_1^5} = P_1 \frac{N_2^3}{N_1^3}$$

B. Delivery Pipe System:

1. Develop H_{syst} Curve

$$2. H_{syst} = H_{stat} + \sum h_L$$

$$3. \sum h_L = h_{L_f} + h_{L_m}$$

$$4. h_{L_f} = f \frac{L}{d^5} \frac{16}{\pi^2} \frac{Q^2}{2g}$$

$$5. h_{L_m} = k \frac{Q^2}{A^2} \frac{1}{2g} = (K_v + 3K_b) \frac{Q^2}{A^2} \frac{1}{2g}$$

$$6. Q = AV = \frac{\pi d^2}{4} V$$

$$7. V = \frac{R\mu}{\rho d}$$

8. Go to Moody chart; find R

9. Assume f

$$10. \frac{e}{d}$$

Problem Statement:

Water at 20°C is to be pumped from a lower reservoir to a higher reservoir through a 30m long, 150mm diameter delivery pipe made of PVC (roughness height, $e = 0.0015\text{mm}$) which is fitted with a fully open gate valve and three threaded 90° elbows. Head loss in the intake pipe can be neglected. The elevation difference between the water surfaces in the two reservoirs will be 10.0m .

Two pumps with the following characteristic data at an operating speed of 800rpm are considered for the project.

Q (lit/s)	Pump 1		Pump 2	
	h_p (m)	η (%)	h_p (m)	η (%)
0	20.0	0	18.0	0
100	19.5	35	17.3	50
200	18.2	54	15.5	68
300	15.9	63	13.5	71
400	12.5	71	10.7	66
500	8.3	68	7.2	47
600	3.0	56	2.0	33

1. Select between the two pumps [show necessary plots]
2. Determine the power required to operate the selected pump
3. Determine the setting for the selected pump. Both pumps have the same cavitations characteristic (σ) equal to 0.6
4. Prepare the characteristic curves for the selected pump if it is operated at a speed of 1200rpm

Given:**A. Pump System:**

Q (lit/s)	Pump 1		Pump 2	
	h_p (m)	η (%)	h_p (m)	η (%)
0	20.0	0	18.0	0
100	19.5	35	17.3	50
200	18.2	54	15.5	68
300	15.9	63	13.5	71
400	12.5	71	10.7	66
500	8.3	68	7.2	47
600	3.0	56	2.0	33

$$N_1 = 800 \text{ rpm}$$

$$N_2 = 1200 \text{ rpm}$$

$\sigma = 0.6$ for both the pumps

B. Reservoirs and delivery pipe system:

$$H_{stat} = 10m$$

$$T_{water} = 20^\circ\text{C}$$

$$L_{pipe} = 30m$$

$$d_{pipe} = 150mm$$

PVC pipe

$$e = 0.0015mm$$

Fitted with a Fully open gate valve

Fitted with 3 threaded 90° elbow

$$h_{L_i} = 0$$

To Find:

1. *Pump 1 or Pump2*
2. *P selected pump*
3. *Z selected pump*
4. *Ch^C selected pump*

Constants:

$T_{water} = 20^\circ\text{C}$ (*given*);

$$\gamma_w = 9789 \frac{N}{m^3}$$

$$\rho_w = 998.2 \frac{kg}{m^3}$$

$$\mu = 1 \times 10^{-3} Pa \cdot s$$

$$P_v = 2.34 \times 10^3 \frac{N}{m^2}$$

$$K_v = 0.2$$

$$K_b = 0.9$$

$$g = 9.80 m/s^2$$

Assume sea level;

$$P_{atm} = 1.013 \times 10^5 - 3.5 \times 10^3 = 97800 N/m^2$$

Conversions:

$$1m^3 = 10^3 \text{ lit.}$$

$$1mm = 10^{-3}m$$

$$1kw = 1000w$$

Calculations:

A. Pump System:

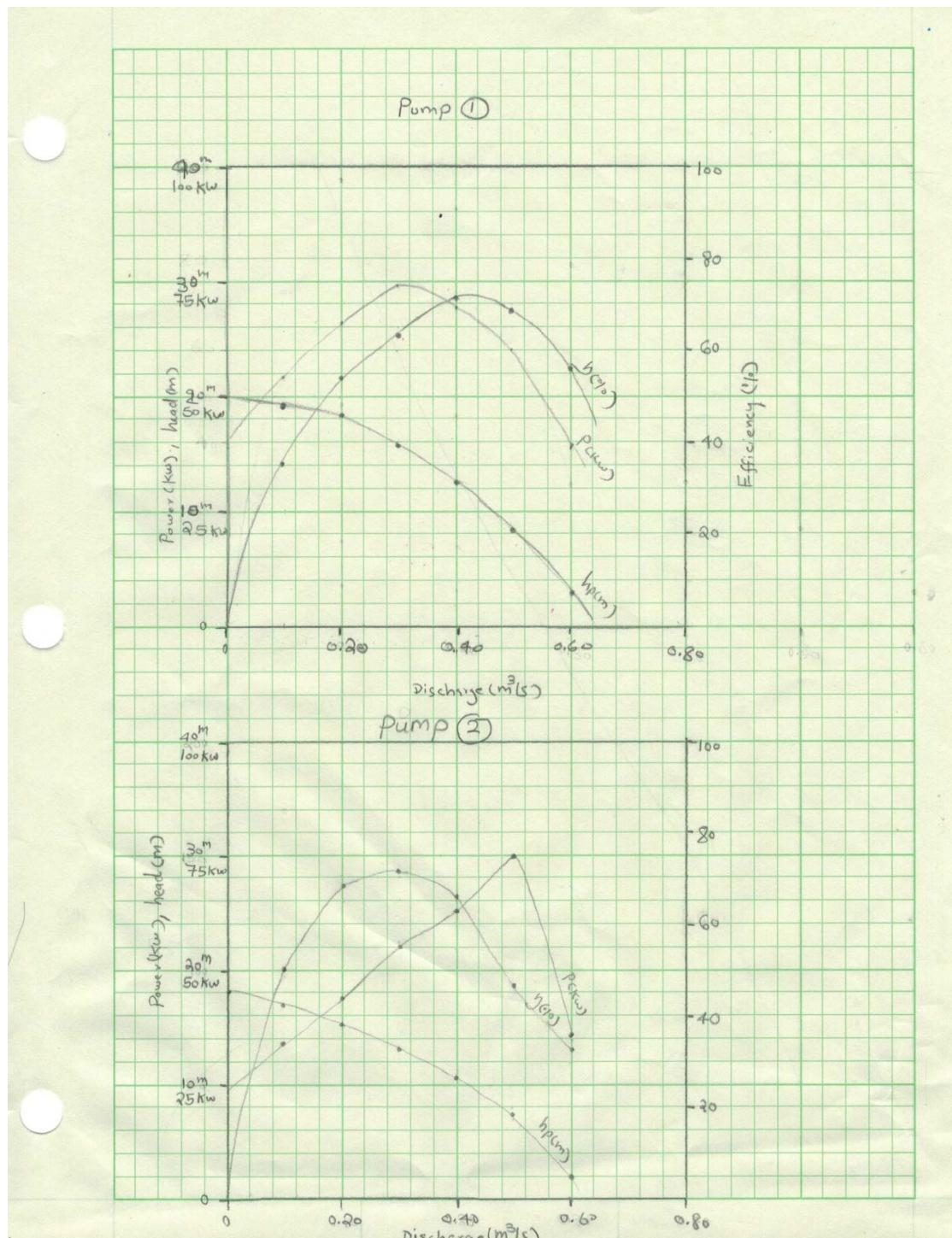
for pump 1: as an example; if $Q = 0.10 \frac{m^3}{s}$, $h_p = 19.5m$, $\eta = 35\%$; then

$$1. P = \frac{(9789)(0.10)(19.5)}{(0.35)} \times \frac{1}{1000} = 54.5 \text{ kw}$$

The following table is the list of other values of P for both pumps

Q (m ³ /s)	Pump 1			Pump 2		
	h_p (m)	η (%)	P(kw)	h_p (m)	η (%)	P(kw)
0	20.0	0	0	18.0	0	0
0.1	19.5	35	54.5	17.3	50	34
0.2	18.2	54	66	15.5	68	44.5
0.3	15.9	63	74	13.5	71	56
0.4	12.5	71	69	10.7	66	63.5
0.5	8.3	68	60	7.2	47	75
0.6	3.0	56	31.5	2.0	33	35.5

2. Characteristic curves ($N = 800 \text{ rpm}$) (Chart #1)



B. Delivery Pipe System:

$$10. \frac{e}{d} = \frac{0.0015}{150} = 1.0 \times 10^{-5}$$

9. Assume $f = 0.012$

8. Go to Moody chart; find $R = 9.5 \times 10^5$

$$7. V = \frac{(9.5 \times 10^5)(1 \times 10^{-3})}{(998.2)(150 \times 10^{-3})} = 6.34 \text{ m/s}$$

$$6. Q = \frac{\pi(150 \times 10^{-3})^2}{4} (6.34) = 0.11 \text{ m}^3/\text{s}$$

$$5. h_{Lm} = (0.2 + 3 \times 0.9) \frac{(0.11)^2}{\pi(150 \times 10^{-3})^2 / 4} \frac{1}{2(9.80)} = 0.10 \text{ m}$$

$$4. h_{Lf} = (0.012) \frac{(30)}{(150 \times 10^{-3})^5} \frac{16}{\pi^2} \frac{(0.11)^2}{2(9.80)} = 4.74 \text{ m}$$

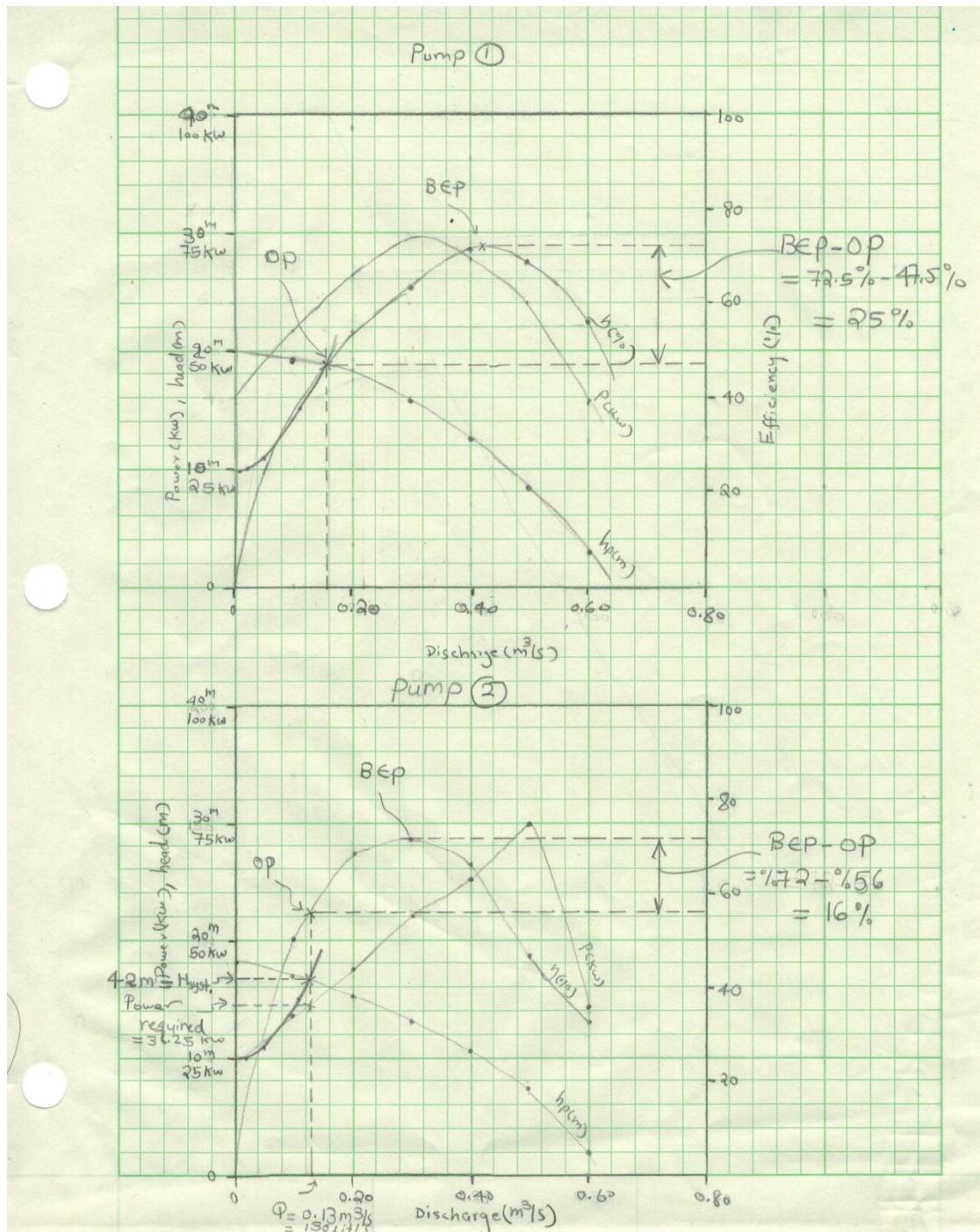
$$3. \sum h_L = 4.74 + 0.10 = 4.84 \text{ m}$$

$$2. H_{syst} = 10 + 4.84 = 14.84 \text{ m}$$

1. Develop H_{syst} Curve: The following is a table of listed value of assumed f and obtained value of Q and H_{syst}

f	R	$V(\text{m/s})$	$Q(\text{m}^3/\text{s})$	$h_{Lm}(\text{m})$	$h_{Lf}(\text{m})$	$\sum h_L(\text{m})$	$H_{stat}(\text{m})$	$H_{syst}(\text{m})$
0.012	9.5×10^5	6.34	0.11	0.1	4.74	4.84	10	14.84
0.014	4×10^5	2.670	0.047	0.018	1.010	1.028	10	11.028
0.016	2×10^5	1.340	0.024	0.005	0.300	0.305	10	10.305
0.018	1×10^5	0.670	0.012	0.001	0.085	0.086	10	10.086
0.020	6×10^4	0.400	0.0071	0.000	0.033	0.033	10	10.033
0.022	4×10^4	0.270	0.0048	0.000	0.017	0.017	10	10.017

1. H_{syst} Curve plotted on the characteristic curves for both pumps (Chart #2)



1. For Pump 1: From Chart #2

$$BEP = 72.5\%$$

$$OP = 47.5\%$$

$$BEP - OP = 72.5\% - 47.5\% = 25\%$$

- For Pump 2: From Chart #2

$$BEP = 72\%$$

$$OP = 56\%$$

$$BEP - OP = 72\% - 56\% = 16\%$$

$$16\% < 25\%$$

Hence;

Pump 2 is selected

2. The power required to operate pump 2 (from chart #2);

$$P = 36.25 \text{ kw}$$

3. From chart #2;

$$h_p \text{ at } BEP = 13m$$

$$Z = \frac{97800}{9789} - 0 - \frac{2.34 \times 10^3}{9789} - 0.6(13)$$

$$Z = 1.95m$$

$$4. h_{p2} = h_{p1} \frac{N_2^2}{N_1^2} = (18) \frac{(1200)^2}{(800)^2} = 40.5m$$

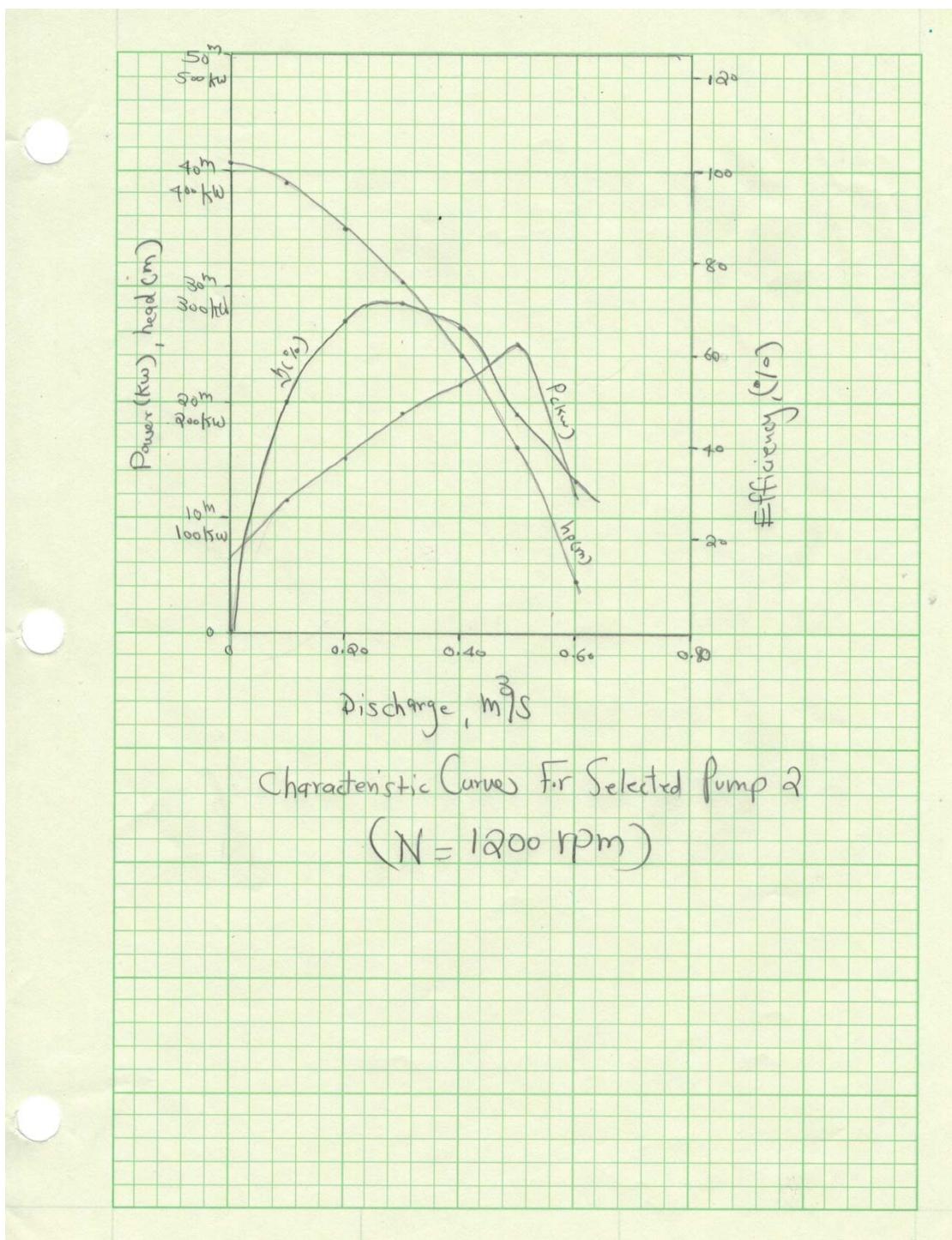
$$P_2 = P_1 \frac{N_2^3}{N_1^3} = (34) \frac{(1200)^3}{(800)^3} = 114.75 \text{ kw}$$

The rest of the values are listed as below;

Pump 2

$Q \text{ (m}^3/\text{s})$	$h_{p1} \text{ (m)}$	$h_{p2} \text{ (m)}$	$P_1 \text{ (kw)}$	$P_2 \text{ (kw)}$	$\eta \text{ (%)}$
0	18.0	40.5	0	0	0
0.1	17.3	39.0	34	115	50
0.2	15.5	35.0	44.5	150	68
0.3	13.5	30.5	56	189	71
0.4	10.7	24.0	63.5	214	66
0.5	7.2	16.0	75	253	47
0.6	2.0	4.5	35.5	120	33

Characteristic Curves for Pump 2 ($N = 1200 \text{ rpm}$)



Conclusion:

After completing the selection process, it has been determined that the second pump is more consistent to be used to be installed on the system. This is because it's efficiency is more optimum than the first pump, that is mean it is capable to get the head required with less operating power. It has been noted that due to the minor and friction head loss the system head is raised up with great amount from the static head (10m) up to about 42 meter.

Bibliography

Houghtalen, Robert J., A. Osman Akan, Ned H. C. Hwang, and Ned H. C. Hwang. Fundamentals of Hydraulic Engineering Systems. 4th ed. Boston: Prentice Hall, 2010. Print.

Miller, Rex, Mark R. Miller, and Harry L. Stewart. Pumps and Hydraulics. 6th ed. Indianapolis, IN: Wiley Pub., 2004. Print.

Properties of Water

Properties of Water^f (SI Metric Units)

Temperature (°C)	Specific Weight ^a γ (kN/m ³)	Density ^a ρ (kg/m ³)	Absolute Dynamic Viscosity ^a μ (Pa·s)	Kinematic Viscosity ^a ν (m ² /s)	Vapor Pressure ^e P_v (kPa)
0	9.805	999.8	0.001781	0.000001785	0.61
5	9.807	1000.0 ^b	0.001518	0.000001518	0.87
10	9.804	999.7	0.001307	0.000001306	1.23
15	9.798	999.1	0.001139	0.000001139	1.70
20	9.789	998.2	0.001002	0.000001003	2.34
25	9.777	997.0	0.000890	0.000000893	3.17
30	9.764	995.7	0.000798	0.000000800	4.24
40	9.730	992.2	0.000653	0.000000658	7.38
50	9.689	988.0	0.000547	0.000000553	12.33
60	9.642	983.2	0.000466	0.000000474	19.92
70	9.589	977.8	0.000404	0.000000413	31.16
80	9.530	971.8	0.000354	0.000000364	47.34
90	9.466	965.3	0.000315	0.000000326	70.10
100	9.399	958.4	0.000282	0.000000294	101.33

Properties of Water (English Units)

Temperature (°F)	Specific Weight γ (lbf/ft ³)	Mass Density ρ (lbf·sec ² /ft ⁴)	Absolute Dynamic Viscosity μ ($\times 10^{-5}$ lbf·sec/ft ²)	Kinematic Viscosity ν ($\times 10^{-5}$ ft ² /sec)	Vapor Pressure P_v (psi)
32	62.42	1.940	3.746	1.931	0.09
40	62.43	1.940	3.229	1.664	0.12
50	62.41	1.940	2.735	1.410	0.18
60	62.37	1.938	2.359	1.217	0.26
70	62.30	1.936	2.050	1.059	0.36
80	62.22	1.934	1.799	0.930	0.51
90	62.11	1.931	1.595	0.826	0.70
100	62.00	1.927	1.424	0.739	0.95
110	61.86	1.923	1.284	0.667	1.24
120	61.71	1.918	1.168	0.609	1.69
130	61.55	1.913	1.069	0.558	2.22
140	61.38	1.908	0.981	0.514	2.89
150	61.20	1.902	0.905	0.476	3.72
160	61.00	1.896	0.838	0.442	4.74
170	60.80	1.890	0.780	0.413	5.99
180	60.58	1.883	0.726	0.385	7.51
190	60.36	1.876	0.678	0.362	9.34
200	60.12	1.868	0.637	0.341	11.52
212	59.83	1.860	0.593	0.319	14.70

^fFrom "Hydraulic Models," ASCE Manual of Engineering Practice, No. 25, ASCE, 1942.

^aFrom J.H. Keenan and F.G. Keyes, *Thermodynamic Properties of Steam*, John Wiley & Sons, 1936.

^bCompiled from many sources including those indicated: *Handbook of Chemistry and Physics*, 54th ed., The CRC Press, 1973, and *Handbook of Tables for Applied Engineering Science*, The Chemical Rubber Co., 1970.

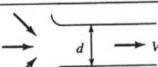
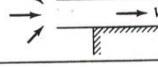
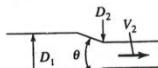
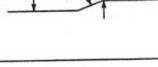
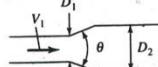
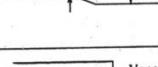
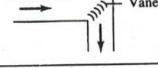
Vennard, J.K. and Robert L. Street, *Elementary Fluid Mechanics*, 6th ed., 1982. Reproduced with permission of John Wiley & Sons.

Loss Coefficients for Transitions and Fittings

5-3 Head Loss 237

$$\begin{aligned}
 P &= \frac{\rho \gamma h_t}{550} \\
 &= 12 \cdot \left[\left(\pi \cdot \frac{10^2}{2} \right) + (20 \cdot 10) \right] \cdot 62.4 \cdot \frac{1948.5}{550} \\
 &= 947,000 \text{ hp}
 \end{aligned}$$

Table 5-3 Representative Loss Coefficients for Various Transitions and Fittings

Description	Sketch	Additional Data	K	Source
Pipe entrance		r/d 0.0 0.1 >0.2	K_e 0.50 0.12 0.03	(7)
				
			1.00	
Contraction		D_2/D_1 0.0 0.20 0.40 0.60 0.80 0.90	K_c $\theta = 60^\circ$ 0.08 0.08 0.07 0.06 0.05 0.04	K_c $\theta = 180^\circ$ 0.50 0.49 0.42 0.32 0.18 0.10
				
Expansion		D_1/D_2 0.0 0.20 0.40 0.60 0.80	K_E $\theta = 10^\circ$ 1.00 0.92 0.72 0.42 0.16	K_E $\theta = 180^\circ$
				
90° miter bend		Without vanes With vanes	$K_b = 1.1$ $K_b = 0.2$	(42)
				
Smooth bend		r/d 1 2 4 6	K_b $\theta = 45^\circ$ 0.10 0.09 0.10 0.12	K_b $\theta = 90^\circ$ 0.35 0.19 0.16 0.21
Threaded pipe fittings		Globe valve - wide open Angle valve - wide open Gate valve - wide open Gate valve - half open Return bend Tee 90° elbow 45° elbow	$K_v = 10.0$ $K_v = 5.0$ $K_v = 0.2$ $K_v = 5.6$ $K_b = 2.2$ $K_b = 1.8$ $K_b = 0.9$ $K_b = 0.4$	(22) and (30)

Physical Properties of Water

Physical Properties of Water

English Units^t

TEMPERATURE, °F	SPECIFIC WEIGHT, γ lb/in. ³	DENSITY, ρ , slug/ft ³	VAPOR PRESSURE, P_v , psia ⁺
32	62.42	1.940	0.09
40	62.43	1.940	0.12
50	62.41	1.940	0.18
60	62.37	1.938	0.26
70	62.30	1.936	0.36
80	62.22	1.934	0.51
90	62.11	1.931	0.70
100	62.00	1.927	0.85
110	61.88	1.923	1.27
120	61.71	1.918	1.69
130	61.55	1.913	2.22
140	61.38	1.908	2.89
150	61.20	1.902	3.72
160	61.00	1.895	4.74
170	60.80	1.890	5.99
180	60.58	1.883	7.51
190	60.36	1.876	9.34
200	60.12	1.868	11.52
212	59.83	1.860	14.70

S.I. Units^t

TEMPERATURE, °C	SPECIFIC WEIGHT, γ kN/m ³	DENSITY, ρ , kg/m ³	VAPOR PRESSURE, P_v , kN/m ²
0	9.805	999.8	0.61
5	9.807	999.0	0.87
10	9.804	999.7	1.23
15	9.798	999.1	1.70
20	9.799	998.2	2.34
25	9.777	997.0	3.17
30	9.764	995.7	4.24
40	9.730	992.2	7.38
50	9.689	988.0	12.33
60	9.642	983.2	19.92
70	9.589	977.8	31.16
80	9.530	971.8	47.34
90	9.468	965.3	70.10
100	9.399	958.4	101.33

Properties of the U.S. Standard Atmosphere

Altitude (ft)	Temperature (°F)	Pressure, p [lb/in. ² (abs)]
-5,000	76.84	17.554
0	59.00	14.696
5,000	41.17	12.228
10,000	23.36	10.108
15,000	5.55	8.297
20,000	-12.26	6.759
25,000	-30.03	5.461
30,000	-47.83	4.373
35,000	-65.61	3.468
40,000	-69.70	2.730
45,000	-69.70	2.149
50,000	-69.70	1.692
60,000	-69.70	1.049
70,000	-67.42	0.651
80,000	-61.98	0.406
90,000	-56.54	0.255
100,000	-51.10	0.162
150,000	-19.40	0.020
200,000	-19.78	0.003
250,000	-88.77	0.000

Properties of the U.S. Standard Atmosphere

Altitude (m)	Temperature (°C)	Pressure, p [N/m ² (abs)]
-1,000	21.50	1.139 E + 5
0	15.00	1.013 E + 5
1,000	8.50	8.988 E + 4
2,000	2.00	7.950 E + 4
3,000	-4.49	7.012 E + 4
4,000	-30.98	6.166 E + 4
5,000	-17.47	5.405 E + 4
6,000	-29.96	4.722 E + 4
7,000	-30.45	4.111 E + 4
8,000	-36.94	3.565 E + 4
9,000	-43.42	3.080 E + 4
10,000	-49.90	2.650 E + 4
15,000	-56.50	1.211 E + 4
20,000	-56.50	5.529 E + 3
25,000	-51.60	2.549 E + 3
30,000	-46.64	1.197 E + 3
40,000	-22.80	2.871 E - 2
50,000	-2.50	7.978 E - 1
60,000	-26.13	2.196 E - 1
70,000	-53.57	5.221 E - 1
80,000	-74.51	1.052 E + 0

for pump calculations,
values of p are reduced by
 0.57 psi
(3.5 kPa)
to account for storm activity.

Moody Chart

